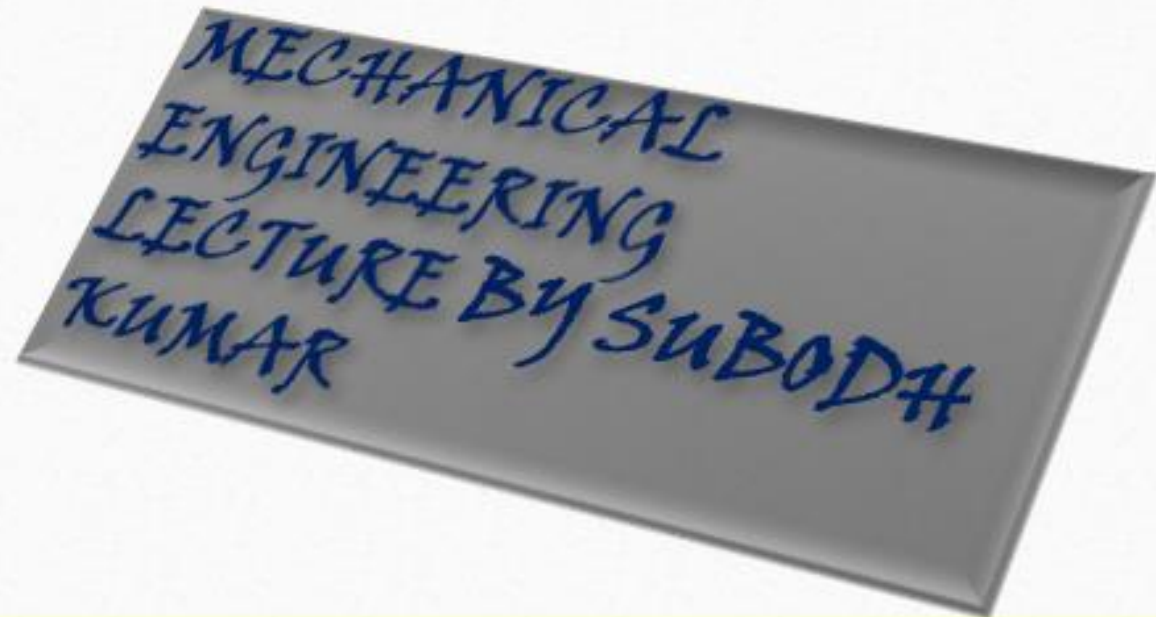




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Viscosity

- Viscosity is defined as the property of a fluid which offers resistance to the movement of one layer of fluid over another adjacent layer of the fluid.
- For liquids, it corresponds to the informal concept of "thickness": for example, syrup has a higher viscosity than water.
- To think of viscosity in everyday terms, the easier a fluid moves, the lower the viscosity. Using our earlier example, which fluid has a greater viscosity? Honey would move slower than water, so honey would have a greater viscosity.



- When two layers of a fluid, a distance 'dy' apart move one over the other at different velocities say u and u+ du as shown in Fig. 1 , the viscosity together with relative velocity causes a shear stress acting between the fluid layers:
- The top layer causes a shear stress on the adjacent lower layer while the lower layer causes a shear stress on the adjacent top layer.
- This shear stress is proportional to the rate of change of velocity with respect to y. It is denoted by symbol τ called Tau.

$$\tau \propto \frac{du}{dy}$$

$$\tau = \mu \frac{du}{dy}$$

$$\mu = \frac{\tau}{\frac{du}{dy}}$$

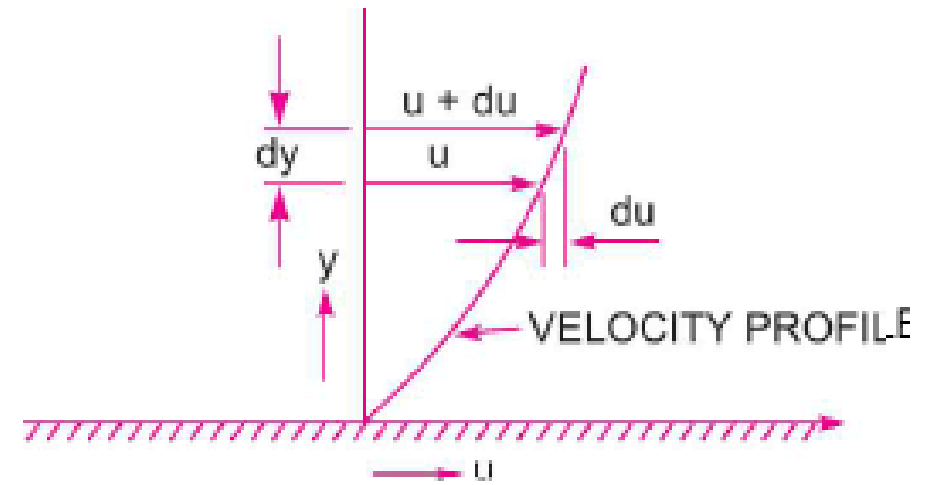


Fig 1 .Velocity variation near a solid boundary

Where,

μ = Viscosity

τ = Shear stress = F/A

$\frac{du}{dy}$ = Rate of shear deformation

- where μ (called mu) is the constant of proportionality and is known as the coefficient of dynamic viscosity or only viscosity.
- $\frac{du}{dy}$ represents the rate of shear strain or rate of shear deformation or velocity gradient.

Unit of Dynamic viscosity

$$\tau = \mu \frac{du}{dy}$$

$$\mu = \frac{\tau}{\frac{du}{dy}} = \frac{\text{Shear Stress}}{\text{Rate of Strain}}$$

In SI

$$= \frac{\text{N/m}^2}{\frac{\text{m/s}}{\text{m}}}$$

Unit of Dynamic Viscosity (μ) = $\frac{\text{Ns}}{\text{m}^2}$

$$= \frac{\text{N}}{\text{m}^2} \times \frac{\text{m}}{\text{s}} = \frac{\text{N}}{\text{m}^2} \times \frac{\text{s}}{1}$$

In SI

$$\mu = \frac{\text{N} \cdot \text{s}}{\text{m}^2}$$

$$\boxed{\mu = \text{Pa} \cdot \text{s}} \quad \text{--- In SI}$$

$$1 \text{ Pa} = \frac{1 \text{ N}}{\text{m}^2}$$

$$1 \text{ Poise} = \frac{1}{10} \frac{\text{Ns}}{\text{m}^2}$$

$$1 \text{ Poise} = \frac{1}{10} \text{ Pa} \cdot \text{s}$$

$$10 \text{ Poise} = 1 \frac{\text{Ns}}{\text{m}^2}$$

Kinematic Viscosity.

- It is defined as the ratio between the dynamic viscosity and density of fluid. It is denoted by the Greek symbol (ν) called 'nu' .

Thus, mathematically,

$$\nu = \frac{\text{Viscosity}}{\text{Density}} = \frac{\mu}{\rho}$$

- The SI unit of kinematic viscosity is m^2/s .

Unit of kinematic viscosity

$$\nu = \frac{\text{viscosity}}{\text{Density}} = \frac{\eta}{\rho}$$

$$= \frac{\frac{\text{Ns}}{\text{m}^2}}{\frac{\text{kg}}{\text{m}^3}}$$

$$= \frac{\text{Ns}}{\text{m}^2} \times \frac{\text{m}^3}{\text{kg}}$$

$$= \frac{\text{Ns m}}{\text{kg}}$$

$$= \frac{\cancel{\text{kg}} \cdot \frac{\text{m}}{\text{s}^2} \times \text{s} \times \text{m}}{\cancel{\text{kg}}}$$

$$\left. \begin{array}{l} 1 \text{ N} = 1 \text{ kg} \cdot 1 \frac{\text{m}}{\text{s}^2} \\ \text{unit} \uparrow \quad \uparrow \quad \uparrow \\ F = m a \\ \text{(Second Law of Newton)} \end{array} \right\}$$

$$\boxed{\text{unit of } \nu = \frac{\text{m}^2}{\text{s}}}$$

MKS & SI unit or in CGS
 cm^2/s
Stokes.

Kinematic viscosity is also known

$$\boxed{1 \text{ Stokes} = 10^{-4} \frac{\text{m}^2}{\text{s}}}$$

Newton's Law of Viscosity.

- It states that the shear stress (τ) on a fluid element layer is directly proportional to the rate of shear strain. The constant of proportionality is called the co-efficient viscosity

$$\tau \propto \frac{du}{dy}$$

$$\tau = \mu \frac{du}{dy}$$

- Fluid which obey the above relation are known as Newtonian fluids and fluid which do not obey the above relation are called Non-Newtonian fluid.

THANKYOU